

# Intrusion Tolerance for Networked Systems through Two-Level Feedback Control

CDIS Spring Conference, 22 May 2024

Kim Hammar (kimham@kth.se) Rolf Stadler (stadler@kth.se)

Center for Cyber Defense and Information Security (CDIS)  
KTH Royal Institute of Technology

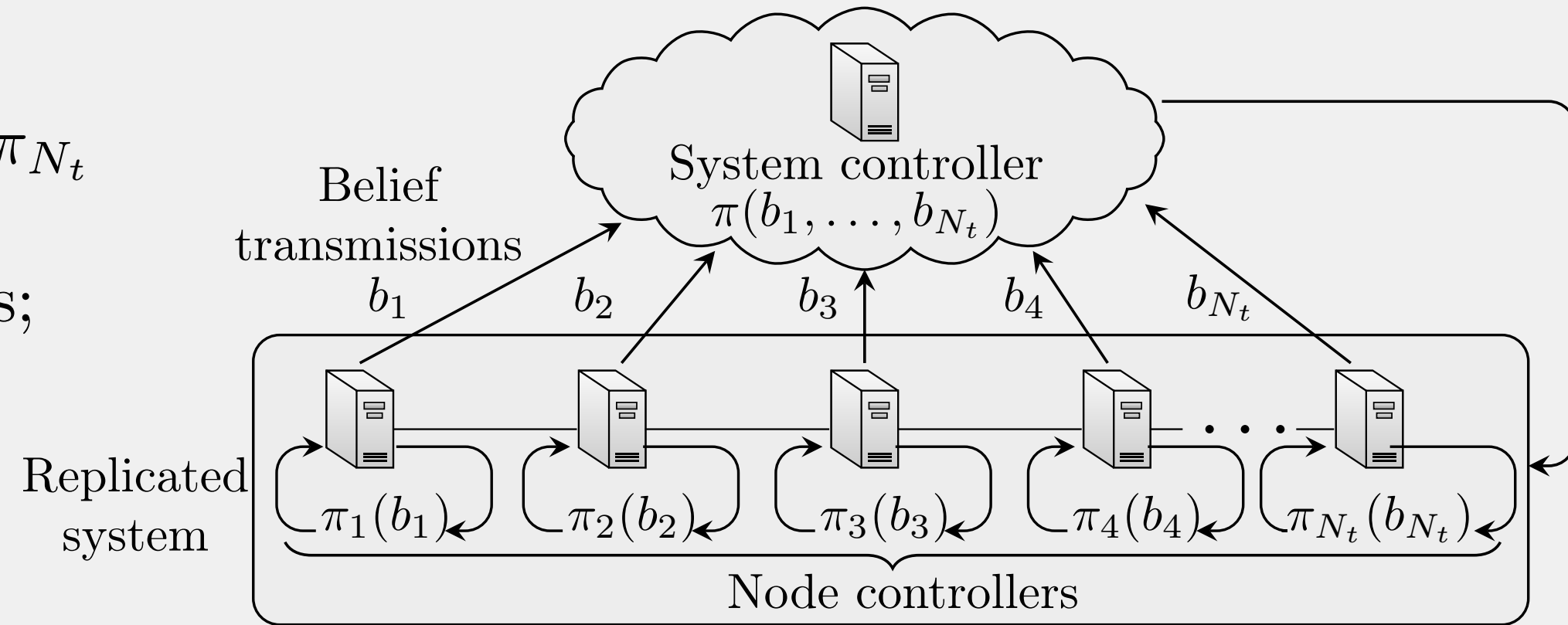


## Contributions

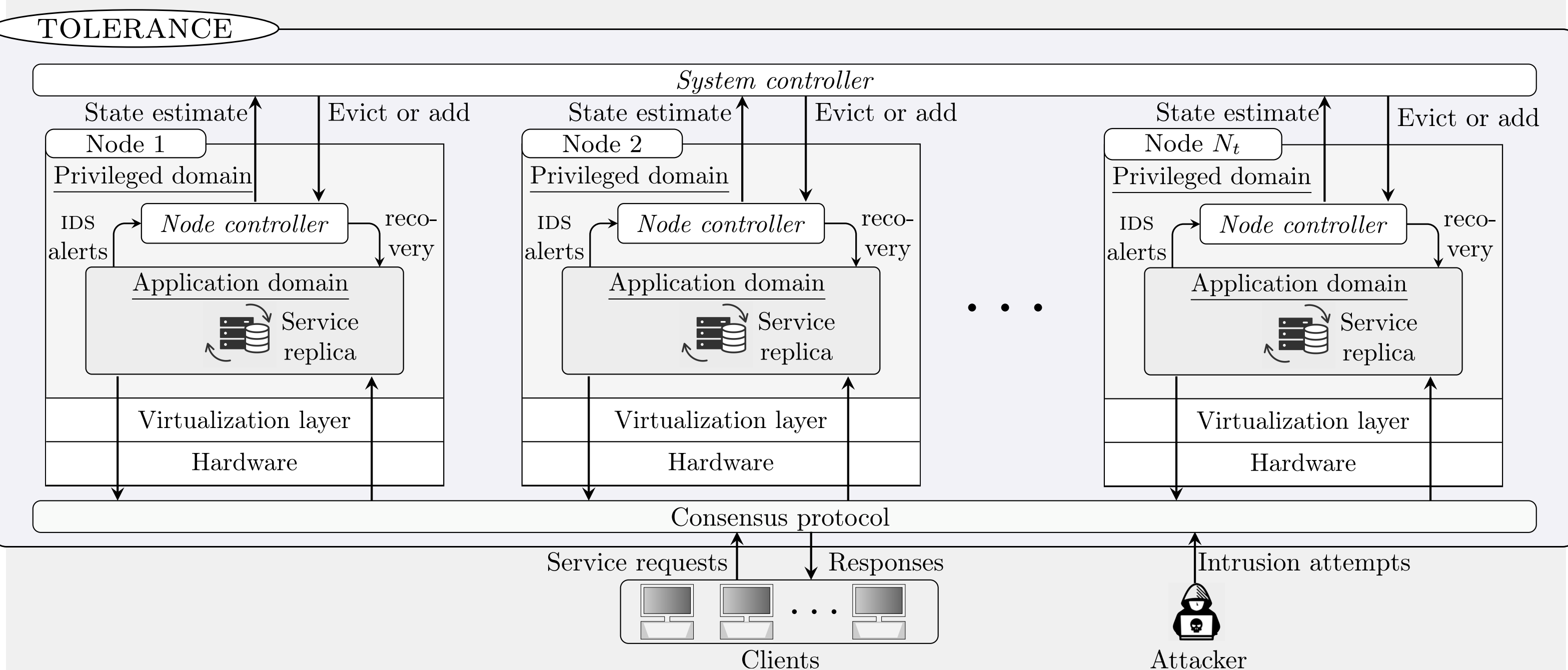
1. We present TOLERANCE, a **control architecture for intrusion-tolerant systems**.
2. We prove properties of the optimal control strategies and design efficient algorithms for computing them.

## Two-level Feedback Control

Node controllers  $\pi_1, \dots, \pi_{N_t}$  compute  $b_1, \dots, b_{N_t}$  and make recovery decisions; a system controller  $\pi$  manages the replication factor  $N_t$ .



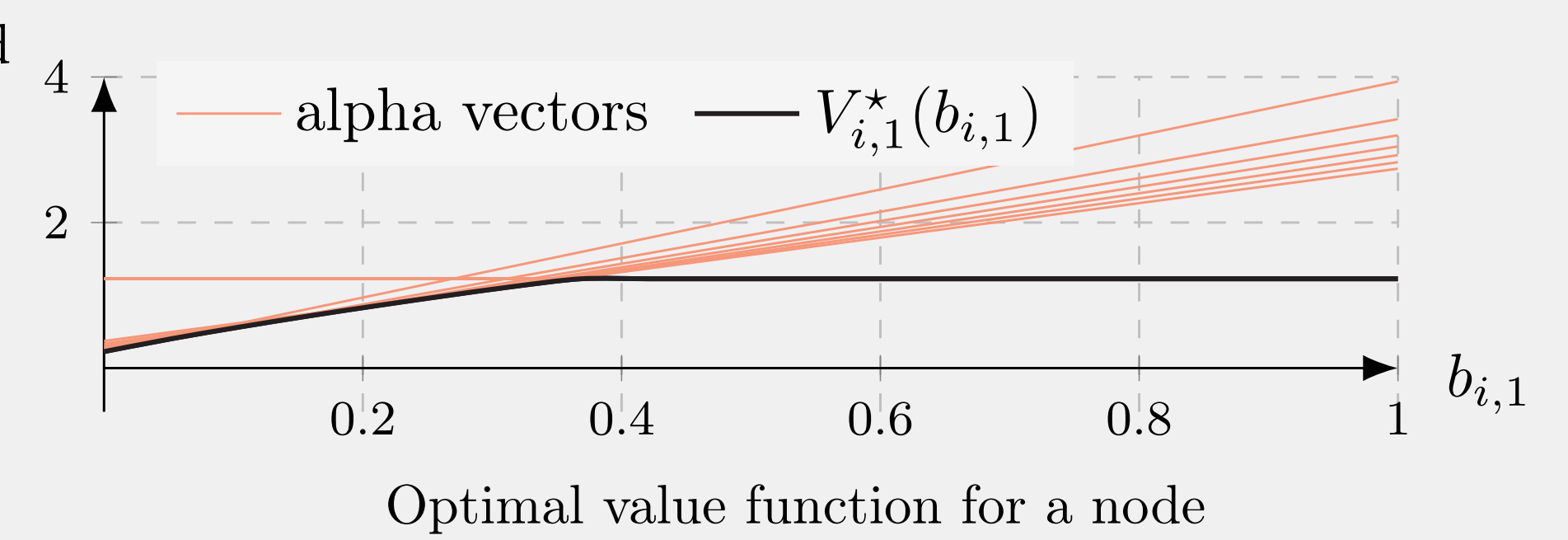
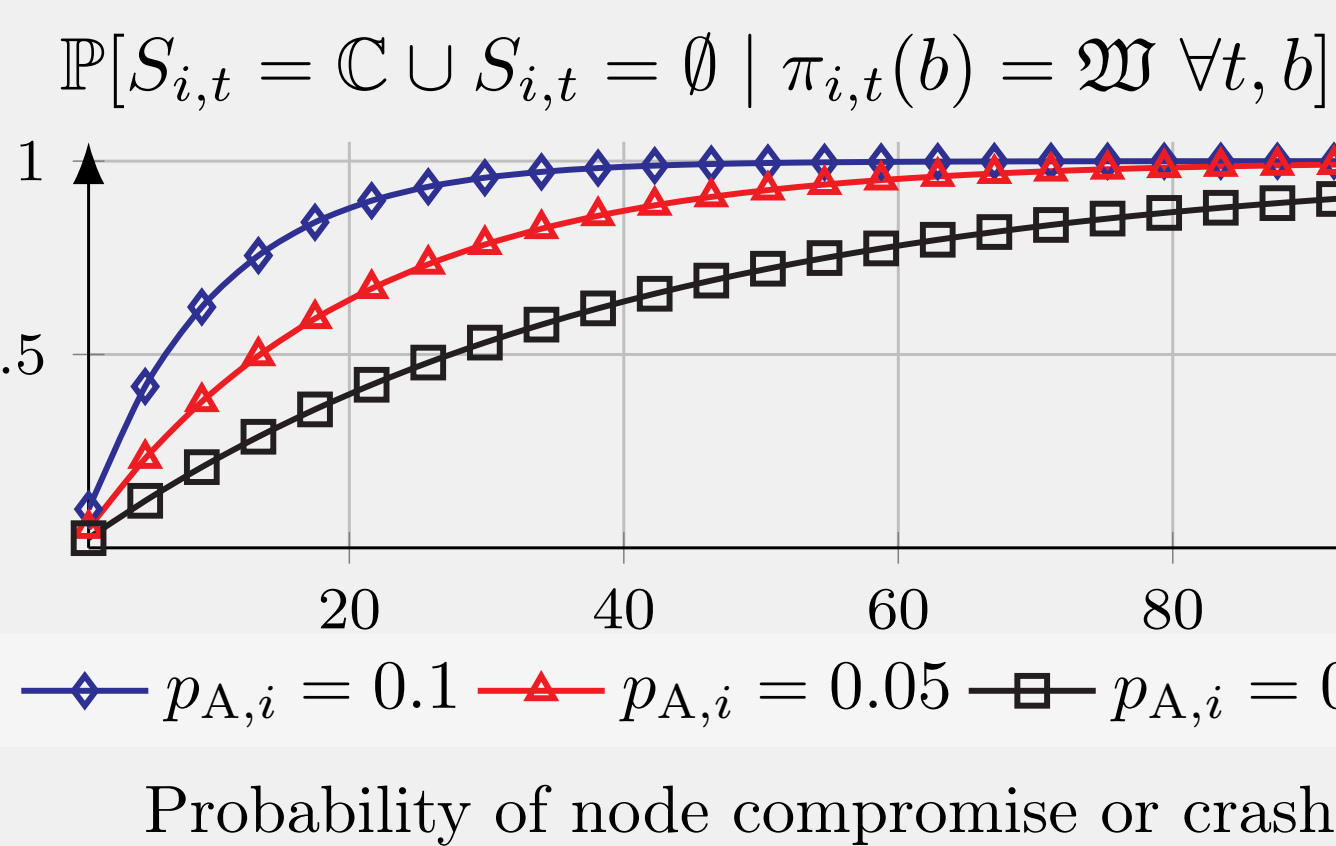
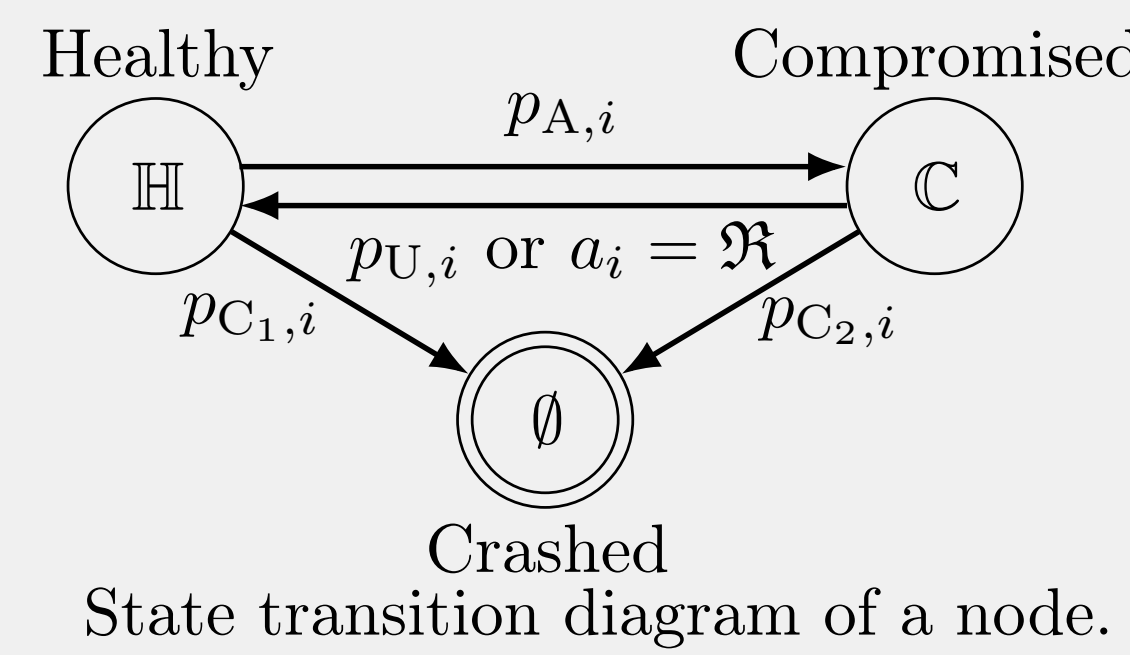
## The TOLERANCE Architecture



**Proposition 1.** TOLERANCE provides **correct service** if the following holds:

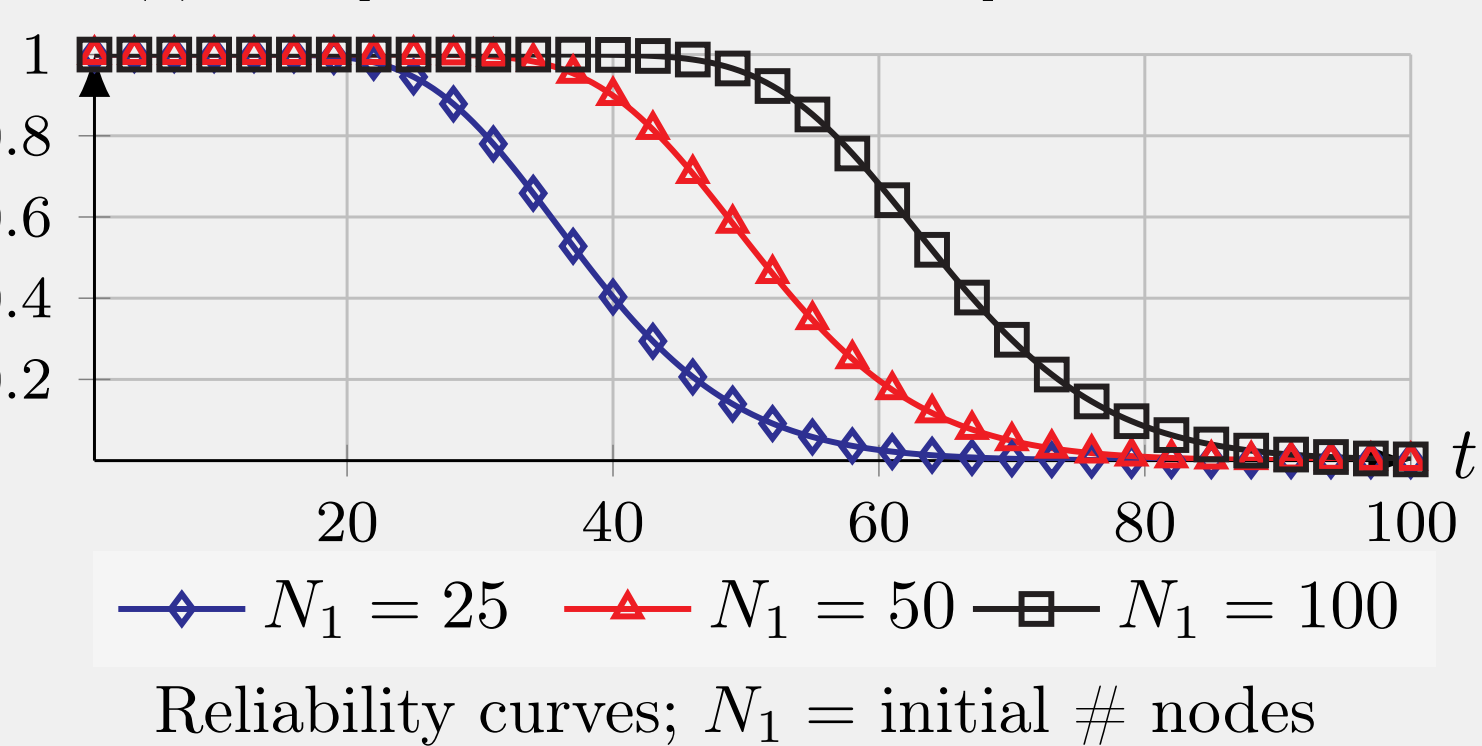
- (a) An attacker can not forge digital signatures.
- (b) Network links are authenticated and reliable.
- (c) At most  $k$  nodes recover simultaneously and at most  $f$  nodes are compromised or crashed simultaneously.
- (d)  $N_t \geq 2f + 1 + k$  at all times  $t$ .
- (e) The system is partially synchronous.

## Formal Model of Intrusion Tolerance



Optimal value function for a node

$$R(t) \triangleq \mathbb{P}[\text{Time of failure} > t]$$



Reliability curves;  $N_1 = \text{initial \# nodes}$

## Structural Results of Optimal Control Strategies

**Theorem 1.** There exists an optimal **recovery strategy**  $\pi_{i,t}^*$  for each node  $i$  that satisfies

$$\pi_{i,t}^*(b_{i,t}) = \mathfrak{R} \iff b_{i,t} \geq \alpha_{i,t}^* \quad \forall t, \quad (1)$$

where  $\alpha_{i,t}^* \in [0, 1]$  is a threshold.

**Corollary 1.** The thresholds satisfy  $\alpha_{i,t+1}^* \geq \alpha_{i,t}^*$  for  $t \in [k\Delta_R, (k+1)\Delta_R]$  and  $i \in \mathcal{N}$ . As  $\Delta_R \rightarrow \infty$ , all thresholds converge to  $\alpha_i^*$ , which is time-independent. ( $\Delta_R$  is the bounded-time-to-recovery (BTR) constraint.)

**Theorem 2.**

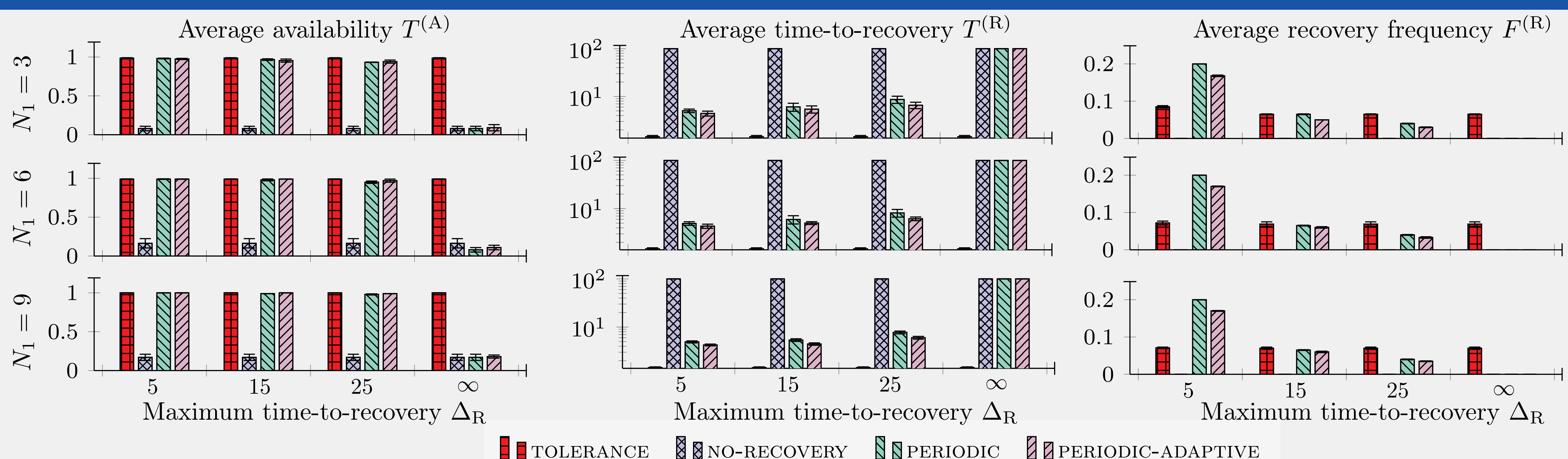
There exist an optimal **replication strategy**  $\pi^*$  that satisfies

$$\pi^*(s_t) = \kappa \pi_{\lambda_1}(s_t) + (1 - \kappa) \pi_{\lambda_2}(s_t) \quad \forall t, s_t \in \mathcal{S}_S \quad (2)$$

for some probability  $\kappa \in [0, 1]$ , where  $\lambda_1, \lambda_2$  are Lagrange multipliers and  $\pi_{\lambda_1}, \pi_{\lambda_2}$  are threshold strategies.

**Consequence of the structural results:** the optimal control strategies can be computed efficiently.

## Comparison to State-of-the-art Intrusion-Tolerant Systems



## Statistical Intrusion Detection

